Acta Crystallographica Section B
Structural
Science
ISSN 0108-7681

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# Associations of squaric acid and its anions as multiform building blocks of hydrogen-bonded molecular crystals 

Squaric acid, $\mathrm{H}_{2} \mathrm{C}_{4} \mathrm{O}_{4}\left(\mathrm{H}_{2} \mathrm{SQ}\right)$, is a completely flat diprotic acid that can crystallize as such, as well as in three different anionic forms, i.e. $\mathrm{H}_{2} \mathrm{SQ} \cdot \mathrm{HSQ}^{-}, \mathrm{HSQ}^{-}$and $\mathrm{SQ}^{2-}$. Its interest for crystal engineering studies arises from three notable factors: (i) its ability of donating and accepting hydrogen bonds strictly confined to the molecular plane; (ii) the remarkable strength of the $\mathrm{O}-\mathrm{H} \cdots \mathrm{O}$ bonds it may form with itself which are either of resonance-assisted (RAHB) or negative-chargeassisted $[(-) \mathrm{CAHB}]$ types; (iii) the ease with which it may donate a proton to an aromatic base which, in turn, back-links to the anion by strong low-barrier $\mathrm{N}-\mathrm{H}^{+} \ldots \mathrm{O}^{1 / 2-}$ chargeassisted hydrogen bonds. Analysis of all the structures so far known shows that, while $\mathrm{H}_{2} \mathrm{SQ}$ can only crystallize in an extended RAHB-linked planar arrangement and $\mathrm{SQ}^{2-}$ tends to behave much as a monomeric dianion, the monoanion $\mathrm{HSQ}^{-}$displays a number of different supramolecular patterns that are classifiable as $\beta$-chains, $\alpha$-chains, $\alpha$-dimers and $\alpha$ tetramers. Partial protonation of these motifs leads to $\mathrm{H}_{2} \mathrm{SQ} \cdot \mathrm{HSQ}^{-}$anions whose supramolecular patterns include ribbons of dimerized $\beta$-chains and chains of emiprotonated $\alpha$ dimers. The topological similarities between the threedimensional crystal chemistry of orthosilicic acid, $\mathrm{H}_{4} \mathrm{SiO}_{4}$, and the two-dimensional one of squaric acid, $\mathrm{H}_{2} \mathrm{C}_{4} \mathrm{O}_{4}$, are finally stressed.

## 1. Introduction

Squaric acid is a strong biprotic acid that can crystallize as pure $\mathrm{H}_{2} \mathrm{SQ}$ (Semmingsen et al., 1977; Gilli \& Bertolasi, 1990) as well as hydrogen squarate $\left(\mathrm{HSQ}^{-}\right)$or squarate $\left(\mathrm{SQ}^{2-}\right)$ anions, the last two being particularly suited for interacting with a variety of hydrogen-bond donors. $\mathrm{H}_{2} \mathrm{SQ}$ and its anions are almost perfectly flat molecules in view of the $\pi$-conjugation of their $\mathrm{C}-\mathrm{C}$ and $\mathrm{C}-\mathrm{O}$ bonds, and, because of that, their four O atoms behave as planar $\left(s p^{2}\right)$ electron donors of one or two lone pairs (Bertolasi et al., 2001). Resonance is known to stabilize the monoanion (II) (Fig. 1) and, at a greater extent, the dianion (III) with respect to the indissociated acid (I). This increased stabilization accounts for the fact that both $\mathrm{H}_{2} \mathrm{SQ}$ and $\mathrm{HSQ}^{-}$are remarkably strong acids $\left(\mathrm{p} K_{1}=1.2-1.7 ; \mathrm{p} K_{2}=\right.$ 3.2-3.5; Ireland \& Walton, 1967; MacDonald, 1968) with a small difference between the two dissociation constants.

In the last years squaric acid and its anions have been frequently used as counteranions in the preparation of a number of molecular crystals. A search on the CSD (release October 2000; Allen et al., 1979) has given, besides the structure of squaric acid (Semmingsen et al., 1977), 24 and 25 other structures of crystals containing the $\mathrm{HSQ}^{-}$and $\mathrm{SQ}^{2-}$ anions, respectively. Therefore, we are now providing a first
account on the crystal chemistry of these ions and on their ability of organizing, in specific predictable ways, the structures of the molecular crystals they are embedded in. Data collected shows that while $\mathrm{H}_{2} \mathrm{SQ}$ can crystallize in a unique planar arrangement and $\mathrm{SQ}^{2-}$ behaves much as a monomeric dianion, the monoanion $\mathrm{HSQ}^{-}$may display a considerable number of polyanionic supramolecular architectures which are the main subject of the present paper. Figs. 2 and 3 sketch the types of polymeric patterns formed by $\mathrm{H}_{2} \mathrm{SQ}$ and $\mathrm{HSQ}^{-}$in their crystals, while Fig. 4 reports the mean geometries of the $\mathrm{C}_{4} \mathrm{O}_{4}$ frame for these different typologies. Figs. 5-10 display a

(I)

(IIa)

(IIc)


Figure 1
$V B$ forms of $\mathrm{H}_{2} \mathrm{SQ}$ (I), $\mathrm{HSQ}^{-}$(II) and $\mathrm{SQ}^{2-}$ (III) showing the increased stabilization by resonance with the increasing negative charge.
(IV) $\mathrm{H}_{2} \mathrm{SQ}$ : RAHB-1,3-chain (crossed $\beta$-chain)

(VI) (HSQ $)_{n}:(-)$ CAHB-1,2-chain ( $\alpha$-chain)

(VII)(HSQ $)_{2}:(-)$ CAHB-1,2-dimer ( $\alpha$-dimer)



Figure 2
The hydrogen-bonded supramolecular patterns found in crystals of $\mathrm{H}_{2} \mathrm{SQ}$ and its $\mathrm{HSQ}^{-}$anion: (IV) double-resonant $\beta$-chain formed by $\mathrm{H}_{2} \mathrm{SQ}$ (KECYBU06: Semmingsen et al., 1977); (V) resonant $\beta$-chain formed by HSQ $^{-}$(CELCEB: Endres \& Schendzielorz, 1984; FEGLUY and FEGMAF: Brach et al., 1987; NUYFUI: Kolev et al., 1998); (VI) [O$\mathrm{H} \cdots \mathrm{O}]^{-} \alpha$-chain formed by $\mathrm{HSO}^{-}$(HIVQEI: Kolev et al., 1999; KHSQR: Bull et al., 1973; PIQTIS: Kolev, Stahl et al., 1997; SADQUJ: Braga \& Grepioni, 1998; TEHYUA: Angelova et al., 1996; TIWWUR: Karle et al., 1996); (VIIa) the [ $\mathrm{O}-\mathrm{H} \cdots \mathrm{O}]^{-} \alpha$-dimer formed by $\mathrm{HSQ}^{-}$(BOLFUD: Bock et al., 1998; BOQDUG: MacLean et al., 1999; KINKEX: Kanters et al., 1991; TIDCAK: Angelova et al., 1996; TIWXIG: Karle et al., 1996; Bertolasi et al., 2001). (VIIb) The 'perturbed ${ }^{\text {‘ }}[\mathrm{O}-\mathrm{H} \cdots \mathrm{O}]^{-} \alpha$-dimer formed by $\mathrm{HSQ}^{-}$(Bertolasi et al., 2001).
number of actual crystal structures which seem particularly suited for illustrating the specific packing of each arrangement. A summary of the topological aspects of the different patterns encountered is finally reported in Fig. 11.

## 2. Results and discussion

All the polymeric patterns displayed in Figs. 2 and 3 are built up of $\mathrm{H}_{2} \mathrm{SQ}$ (IV) and $\mathrm{HSQ}^{-}$(V)-(VIII) units, or by (IX)-(X) connected by a net of $\mathrm{O}-\mathrm{H} \cdots \mathrm{O}$ bonds whose $d(\mathrm{O} \cdots \mathrm{O})$ distances, or range of distances, in $\AA$ are displayed in italics on the figures in association with each pattern, together with hydrogen-bond symbology (Etter et al., 1990; Bernstein et al., 1995). All $\mathrm{O}-\mathrm{H} \cdots \mathrm{O}$ bonds are remarkably short and presumably strong, laying in the range $2.43 \leq d(\mathrm{O} \cdots \mathrm{O}) \leq$ $2.56 \AA$, which corresponds to a range of hydrogen-bond energies of $38 \leq E_{\mathrm{HB}} \leq 84 \mathrm{~kJ} \mathrm{~mol}^{-1}$ according to the Lippincott \& Schroeder (1955) force field. They are therefore definitely stronger than ordinary $\mathrm{O}-\mathrm{H} \cdots \mathrm{O}$ bonds, such as those connecting the water molecules in ice $[d(\mathrm{O} \cdots \mathrm{O})=$ $2.74 \AA \AA_{\mathrm{HB}} \simeq 17 \mathrm{~kJ} \mathrm{~mol}^{-1}$ ].

Strong homonuclear $\mathrm{O}-\mathrm{H} \cdots \mathrm{O}$ bonds have been fully classified by Gilli et al. (1994) who were able to show, on the grounds of large neutron and X-ray crystal-structure evidence, that there are but three classes of really strong (short) O $\mathrm{H} \cdots \mathrm{O}$ bonds:
(i) (-)CAHBs: $[\mathrm{O}-\mathrm{H} \cdots \mathrm{O}]^{-}$negative-charge-assisted hydrogen bonds $[2.38 \leq d(\mathrm{O} \cdots \mathrm{O}) \leq 2.50 \AA$ § ;


(X) $\left(\mathrm{H}_{2} \text { SQ.HSQ }\right)_{n}^{-}:$(- CAHB-4,4'-chain of 1,2-dimers



Figure 3
Another hydrogen-bonded supramolecular pattern formed by the HSQ ${ }^{-}$ anion: (VIII) the $[\mathrm{O}-\mathrm{H} \cdots \mathrm{O}]^{-} \alpha$-tetramer (RAVWAM: Kolev, Preut et al., 1997). The hydrogen-bonded supramolecular patterns formed in crystals by the $\mathrm{H}_{2} \mathrm{SQ} \cdot \mathrm{HSQ}^{-}$anion: (IX) two resonant $\beta$-chains interconnected by $[\mathrm{O}-\mathrm{H} \cdots \mathrm{O}]^{-}$bonds (Lin et al., 1994); (Xa) [O$\mathrm{H} \cdots \mathrm{O}]^{-} \alpha$-chain of $\mathrm{H}_{2} \mathrm{SQ} \cdot \mathrm{HSQ}^{-}$dimers (SADRAQ: Braga \& Grepioni, 1998); (X $b, c$ ) protonation of the $[\mathrm{O}-\mathrm{H} \cdots \mathrm{O}]^{-} \alpha$-dimer (Xb) with formation of the $\left(\mathrm{H}_{2} \mathrm{SQ} \cdot \mathrm{HSQ}^{-}\right)$anion $(\mathrm{X} c)$.
(ii) (+)CAHBs: $[\mathrm{O}-\mathrm{H} \cdots \mathrm{O}]^{+}$positive-charge-assisted hydrogen bonds $[2.36 \leq d(\mathrm{O} \cdots \mathrm{O}) \leq 2.43 \AA$ ];
(iii) RAHBs: $-\mathrm{O}-\mathrm{H} \cdots \mathrm{O}=$, resonance-assisted hydrogen bonds where the two O atoms are connected by a $\pi$-conjugated system of single and double bonds $[2.39 \leq d(\mathrm{O} \cdots \mathrm{O}) \leq$ $2.55 \AA$ §.

(XI) $\mathrm{H}_{2} \mathrm{SQ}$ : 'Standard' distances

(XII) $\mathrm{H}_{2} \mathrm{SQ}$ : Crystal structure
(XIII) (HSQ $\left.{ }^{-}\right)_{n}: \beta$-Chain


(XIV) $\left(\mathrm{HSQ}^{-}\right)_{\mathrm{n}}: \alpha$-Chain \& Ring

(XVI) $\left(\mathrm{HSQ}^{-}\right)_{2}$ : 'Perturbed' $\alpha$-Dimer by the heteroconjugated $\cdots \mathrm{O}=\mathrm{C}-\mathrm{C}=\mathrm{C}-\mathrm{OH} \cdots \beta$-diketone enol group.
Simple inspection of Figs. 2 and 3 shows that all the O $\mathrm{H} \cdots \mathrm{O}$ bonds formed by $\mathrm{H}_{2} \mathrm{SQ}$ and $\mathrm{HSQ}^{-}$belong to two out of these three classes of strong bonds, i.e. ( - CAHB and RAHB, whose different expressions give rise to the variety of association patterns (IV)-(X) individually described in some detail in the following sections.

## 2.1. $\boldsymbol{\beta}$-Chains: RAHB 1,3-chains (IV) and (V)

$\beta$-Diketone (or 1,3-diketone) enols $\cdots \mathrm{O}=\mathrm{C}-\mathrm{C}=\mathrm{C}-$ $\mathrm{OH} \cdots$ make normally strong intramolecular RAHBs by closing a hydrogen-bonded six-membered ring. When this is forbidden for steric reasons (e.g. in 1,3-cyclopentandione or


$(\mathrm{XV})\left(\mathrm{HSQ}^{-}\right)_{2}: \alpha$-Dimer

Figure 4
Average crystallographic bond distances in $\mathrm{H}_{2} \mathrm{SQ}$ and its $\mathrm{HSQ}^{-}$anions, whose supramolecular patterns are reported in (IV)-(VII) of Fig. 2. The e.s.d's are given in parentheses and e.s.d's from the mean in square brackets. (XI) reports the 'standard' bond distance of $\mathrm{H}_{2} \mathrm{SQ}$ unperturbed by $\pi$-delocalization and hydrogen-bond formation (Gilli et al., 1993).


Figure 5
$\beta$-chain of $\mathrm{HSQ}^{-}$anions surrounded by hydrogen-bonded water molecules free or coordinated in hexa-aquo cobalt anions (FEGMAF: Brach et al., 1987).

Typical (-)CAHBs are the intermolecular RCOOH $\ldots{ }^{-}$OOCR bonds in carboxylic acid-carboxylate complexes, (+)CAHBs those formed by two oxygenated molecules $\quad\left(\mathrm{H}_{2} \mathrm{O} \cdots \mathrm{H}^{+} \cdots \mathrm{OH}_{2}, \quad \quad R_{2} \mathrm{O} \cdots \mathrm{H}^{+} \cdots \mathrm{O} R_{2}\right.$, $\mathrm{Me}_{2} \mathrm{~S}=\mathrm{O} \cdots \mathrm{H}^{+} \cdots \mathrm{O}=\mathrm{SMe}_{2}$ etc.) bridged by a proton donated by a strong acid within the crystal, while the most common cases of RAHB are the strong $-\mathrm{O}-\mathrm{H} \cdots \mathrm{O}=$ bonds formed

Figure 6
$\beta$-chain of $\mathrm{HSQ}^{-}$anions surrounded by hydrogen-bonded water molecules and asparaginium cations (NUYFUI: Kolev et al., 1998).


Figure 7
Isolated $\alpha$-chain of $\mathrm{HSQ}^{-}$anions surrounded by cobaltocenium cations (SADQUJ: Braga \& Grepioni, 1998).

1,3-cyclohexandione enols) molecules crystallize by forming extended RAHB chains (resonant $\beta$-chains; Gilli et al., 1993; Bertolasi et al., 1996).

The molecule of $\mathrm{H}_{2} \mathrm{SQ}$ (I) consists of two $\beta$-diketone enol groups intercrossed along the square diagonals. Accordingly, it crystallizes by making planes of two intersecting $\beta$-chain systems (IV) characterized by short $\mathrm{O}-\mathrm{H} \cdots \mathrm{O}$ RAHBs having $d(\mathrm{O} \cdots \mathrm{O})=2.554$ (1) $\AA$ and by the typical perturbation of the $\mathrm{C}-\mathrm{C}$ and $\mathrm{C}-\mathrm{O}$ bonds shown in (XII) of Fig. 4 (see for a detailed discussion Gilli et al., 1993).

Deprotonated $\mathrm{HSQ}^{-}$can still make one $\left(\mathrm{HSQ}^{-}\right)_{n} \beta$-chain $(\mathrm{V})$, which is actually the superimposition on the same track of two RAHB chains, i.e. $\cdots \mathrm{O}=\mathrm{C} 3-\mathrm{C} 2=\mathrm{C} 1-\mathrm{OH} \cdots$ and $\cdots \mathrm{O}=\mathrm{C} 3-\mathrm{C} 4=\mathrm{C} 1-\mathrm{OH} \cdots$, with the consequent symmetrization of the $\mathrm{C}_{4} \mathrm{O}_{4}$ fragment around the $\mathrm{C} 1 \cdots \mathrm{C} 3$ diagonal shown in (XIII) and with the formation of an $\mathrm{O}-\mathrm{H} \cdots \mathrm{O}$ RAHB of a length strictly comparable to that of $\mathrm{H}_{2} \mathrm{SQ}$ $\left[d(\mathrm{O} \cdots \mathrm{O})\right.$ of $2.55-2.62 \AA$ against $2.55 \AA$ ]. Since the $\mathrm{HSQ}^{-}$ negative charges are not used in $\beta$-chain formation, these negative charges remain confined over the O 2 and O 4 atoms at the borderline of the $\left(\mathrm{HSQ}^{-}\right)_{n}$ chain with formal charges of $\frac{1}{2}-$. Accordingly, the $\beta$-chain is strongly hydrophilic and it is


Figure 8
$\alpha$-chain of $\mathrm{HSQ}^{-}$anions surrounded by hydrogen-bonded water molecules (KHSQUR: Bull et al., 1973).


Figure 9
$\alpha$-chain of $\mathrm{HSQ}^{-}$anions surrounded by hydrogen-bonded imidazolium cations (TIWWUR: Karle et al., 1996).
found, in crystals, to be totally surrounded by water molecules (e.g. FEGMAF: Brach et al., 1987; Fig. 5) or by both water and protonated amines or aminoacids (e.g. NUYFUI: Kolev et al., 1998; Fig. 6).

## 2.2. $\boldsymbol{a}$-Chains: (-)CAHB-1,2 chains (VI)

Besides the $\beta$-diketone enol group that may form $\beta$-chains, the $\mathrm{HSQ}^{-}$ion contains a further ${ }^{-} \mathrm{O}-\mathrm{C} 2=\mathrm{C} 1-\mathrm{OH} \alpha$-diketone enolate (or 1,2-diketone enolate) group suitable for forming $[\mathrm{O}-\mathrm{H} \cdots \mathrm{O}]^{-}(-)$CAHBs, which are even stronger


Figure 10
$\alpha$-dimer of $\mathrm{HSQ}^{-}$anions surrounded by hydrogen-bonded 3-aminopyridinium cations (Bertolasi et al., 2001).


Figure 11
Schemes of the polymeric structures formed by squaric acid and its anions in crystals. The $\mathrm{C}_{4} \mathrm{O}_{4}$ frame is represented as a square and the hydroxyl positions by dots.
than RAHBs. It can form a second type of chain, the $(-)$ CAHB-1,2 chain or $\alpha$-chain (VI) linked by $[\mathrm{O}-\mathrm{H} \cdots \mathrm{O}]^{-}$ bonds having $\mathrm{O} \cdots \mathrm{O}$ distances in the range $2.47-2.55 \AA$, slightly longer than the standard range of $2.38-2.50 \AA$ reported for isolated $(-) \mathrm{CAHBs}$, where the two O atoms do not accept other hydrogen bonds from the environment (Gilli et al., 1994). In $\alpha$-chains the negative charges are localized on the chain itself, in particular on the $[\mathrm{C} 1-\mathrm{OH} \cdots \mathrm{O}-\mathrm{C} 2]^{-}$ bridge, and not delocalized over the chain-environment borderline as in $\beta$-chains. Accordingly, $\alpha$-chains are less hydrophilic than $\beta$-chains and can also occur in non-solvated environments, such as the isolated $\alpha$-chain of cobaltocenium•HSQ ${ }^{-}$(SADQUJ: Braga \& Grepioni, 1998) displayed in Fig. 7, although the cases where the external O atoms are saturated by hydrogen-bond donors [water molecules in KHSQUR: Bull et al., 1973 (Fig. 8); protonated amines in TIWWUR: Karle et al., 1996 (Fig. 9) or both, e.g. HIVQEI: Kolev et al., 1999] are more common.

## 2.3. $\alpha$-Dimers: (-)CAHB-1,2 dimers (VII)

The formation of $\alpha$-dimers (VII) is one of the most common ways of aggregation of $\mathrm{HSQ}^{-}$anions which are now linked by two strong $[\mathrm{O}-\mathrm{H} \cdots \mathrm{O}]^{-}(-)$CAHBs. The observed range of $\mathrm{O} \cdots \mathrm{O}$ distances of 2.47-2.54 $\AA$ is very similar to that found in $\alpha$-chains, although the $\mathrm{O}-\mathrm{H} \cdots \mathrm{O}$ bonds in the latter are normally more linear.

As a crystal structural unit (tecton) the $\alpha$-dimer can sometimes crystallize as an isolated anion (SADRAQ: Braga \& Grepioni, 1998; BOQDUG: MacLean et al., 1999), but normally behaves as a planar 12-lone-pair hydrogen-bond acceptor particularly suited to form co-crystals (mixed crystals) with mostly aromatic nitrogen amines protonated by the dissociation of the squaric acid itself. The structures formed are most frequently planar (e.g. Fig. 10; Bertolasi et al., 2001), although a few cases of three-dimensional associations are also known (Bertolasi et al., 2001; Karle et al., 1996). All structures containing $\alpha$-dimers share the interesting property of being completely anhydrous, in spite of the fact that most of them were crystallized from water. As hydrogen-bond acceptors, the four O atoms of the $\mathrm{HSQ}^{-}$subunit display different behaviours. The carbonylic O 3 atom is only found to be an acceptor of rather weak and neutral $\mathrm{N}-\mathrm{H} \cdots \mathrm{O} 3$ bonds, while positively charged hydrogen-bond donors tend to bind to the O 2 and O 4 atoms. The reason is seen in the resonance schemes (II) (Fig. 1), showing that only these two last atoms are charged and may then form $\mathrm{N}^{+}-\mathrm{H} \cdots \mathrm{O}^{1 / 2-}$ or $\mathrm{N}^{+}-$ $\mathrm{H} \cdots \mathrm{O}^{-}$bonds.

## 2.4. $a$-Dimer relaxation under the external hydrogen-bond field

In the last few years increasing attention has been devoted to hydrogen bonds which can be related to the acid-base equilibrium

$$
\begin{equation*}
\mathrm{AcO}-\mathrm{H} \cdots \mathrm{~N} \equiv \rightleftharpoons \mathrm{AcO}^{-} \cdots \mathrm{H}-\mathrm{N}^{+} \equiv \tag{1}
\end{equation*}
$$

where $\mathrm{N} \equiv$ is a nitrogen base, most frequently aromatic, and AcOH can be an organic (carboxylic acid, phenol, squaric acid) as well as an inorganic acid. It is now generally recognized that:
(i) the proton position $\left(\mathrm{O}-\mathrm{H} \cdots \mathrm{N}\right.$ or $\left.\mathrm{O}^{-} \cdots \mathrm{H}-\mathrm{N}^{+}\right)$is essentially determined by the difference of the gas-phase proton affinities, $\triangle \mathrm{PA}$, or, alternatively, by the corresponding $\Delta \mathrm{p} K_{a}$ in aqueous solution;
(ii) very strong $\mathrm{N}-\mathrm{H} \cdots \mathrm{O}$ bonds (up to $85-105 \mathrm{~kJ} \mathrm{~mol}^{-1}$ ) must be associated with the condition $\triangle \mathrm{PA}$, or $\Delta \mathrm{p} K_{a}$, approaching zero (Malarski et al., 1982; Zeegers-Huyskens, 1991; Sobczyk, 1998; Reinhardt et al., 1998).
These very strong bonds with almost perfect $\mathrm{p} K_{a}$ matching have been given, particularly in the biochemical literature, the name of low-barrier hydrogen bonds (LBHBs) and are supposed to play an important role in some processes of enzymatic catalysis (Cleland, 1992; Cleland \& Kreevoy, 1994; Frey et al., 1994). More recently, all hydrogen bonds derived from equilibrium (1) have been given the alternative name (+/-)CAHB (positive/negative charge-assisted hydrogen bond; Gilli \& Gilli, 2000) in analogy with the already established (+)CAHB, (-)CAHB and RAHB nomenclature (Gilli et al., 1994).

As discussed above, the $\left(\mathrm{HSQ}^{-}\right)_{2} \alpha$-dimer can be an acceptor of $(+/-)$ CAHB formed by the partially charged O 2 and O 4 atoms with protonated nitrogen bases, whose strength is modulated by the $\Delta \mathrm{p} K_{a}$ of the interacting moieties. Most of these bonds are only moderately strong, being in the $\mathrm{N} \cdots \mathrm{O}$ range 2.72-2.78 $\AA$ (Bertolasi et al., 2001; Karle et al., 1996; Endres \& Schendzielorz, 1984), and are found in association with the average geometry of the $\mathrm{C}_{4} \mathrm{O}_{4}$ frame displayed in (XV) (Fig. 4). This is characterized, in analogy with that found for $\alpha$-chains (XIV), by a strong bond dissymmetry around the HO 1 C 1 C 3 O 3 diagonal, in particular as far as the $\mathrm{C} 2-\mathrm{O} 2$ and $\mathrm{C} 4-\mathrm{O} 4$ distances [on average, 1.253 (5) and 1.223 (5) $\AA$ in (XV) and 1.268 (12) and 1.237 (4) $\AA$ in (XIV)] are concerned, in agreement with the idea that the $[\mathrm{O} 1-\mathrm{H} \cdots \mathrm{O} 2]^{-}$bond shifts the tautomeric equilibrium (II) (Fig. 1) towards the form (II $a$ ).

Rather surprisingly, the formation of a single stronger $\equiv \mathrm{N}^{+}-\mathrm{H} \cdots \mathrm{O} 4$ bond having $d(\mathrm{~N} \cdots \mathrm{O})$ of 2.675 (6) $\AA$ (Fig. 10; Bertolasi et al., 2001) seems able to upset such a bonding situation by changing the molecular symmetry from (VII $a$ ) to (VIIb) (Fig. 2) and the bond distances from (XV) to (XVI) (Fig. 4). The new geometry is now almost perfectly diagonalsymmetric with $d(\mathrm{C} 2-\mathrm{O} 2)=d(\mathrm{C} 4-\mathrm{O} 4)=1.240(4) \AA$ and $d(\mathrm{C} 2-\mathrm{C} 3)=d(\mathrm{C} 3-\mathrm{C} 4)=1.488(5) \AA$, on average, with bond distance shifts that can reach $0.027 \AA$. The most straightforward reason for this fact seems to be that the $\mathrm{p} K_{a}(6.0)$ of the aminopyridinium ion (Fig. 10) better matches the unknown $\mathrm{p} K_{a}$ of the $\left(\mathrm{HSQ}^{-}\right)_{2} \alpha$-dimer to form a very strong $\mathrm{N}^{+}-$ $\mathrm{H} \cdots \mathrm{O}^{-}$LBHB. This, in turn, causes a withdrawal of electrons towards O 4 and from the $\alpha$-dimer, which thus changes its ground state from mainly (II $a$ ) (Fig. 1) to an almost perfect
mixture of (II $a$ ) and (IIb), i.e. to (II $c$ ), with final equal sharing of the negative charge between the O 2 and O 4 atoms.

Since symmetrical arrangements can only be energy minima or maxima in the molecular configuration space, it seems reasonable to assume that the diagonal-symmetric geometry (VII $b) /(\mathrm{XVI})$ marks the geometry of the transition state (TS) along the protonation reaction pathways

$$
\begin{equation*}
(\mathrm{X} b) \rightleftharpoons T S \rightleftharpoons(\mathrm{X} c) \tag{2}
\end{equation*}
$$

connecting the two dissymmetric lower-energy states $(\mathrm{X} b)$ and ( Xc ) (Fig. 3).

### 2.5. More complex $\mathrm{HSQ}^{-}$and $\mathrm{H}_{2} \mathrm{SQ} \cdot \mathrm{HSQ}^{-}$polyanions

$\beta$-Chains (V), $\alpha$-chains (VI) and $\alpha$-dimers (VII) can be considered the normal aggregation forms of the $\mathrm{HSQ}^{-}$anion. This anion can, however, associate in other more complex forms that, so far, have not been observed more than once, but that seem to open new interesting perspectives in the design of new squaric acid-based co-crystals.

The simplest case is represented by the $\left(\mathrm{HSQ}^{-}\right)_{4}$ (-)CAHB-1,2 tetrameric ring [or $\alpha$-tetramer (VIII); RAVWAM: Kolev, Preut et al., 1997], whose O-H $\cdots \mathrm{O}$ bonds $\left[2.46 \leq d(\mathrm{O} \cdots \mathrm{O}) \leq 2.49 \AA\right.$ ] and $\mathrm{C}_{4} \mathrm{O}_{4}$ frame geometries are very similar to those for $\alpha$-chains (VI)/(XIV).

More interestingly, the case described in (IX) (Lin et al., 1994) consists of two parallel and antidromic $\beta$-chains, where the monomers are linked by 1,3 -RAHBs with $d(\mathrm{O} \cdots \mathrm{O})=$ 2.564 (1) $\AA$ [strictly similar to those found in $\mathrm{H}_{2} \mathrm{SQ}$ (IV) and $\beta$-chains (V)] transversally connected in pairs by very short and perfectly centered $[\mathrm{O} \cdots \mathrm{H} \cdots \mathrm{O}]^{-} \quad(-) \mathrm{CAHBs}$ with $d(\mathrm{O} \cdots \mathrm{O})=2.432(1) \AA$. Note that the pattern of (IX) is no longer a polyanion of $\mathrm{HSQ}^{-}$, but of the $\mathrm{H}_{2} \mathrm{SQ} \cdot \mathrm{HSQ}^{-}$dimeric anion, having acquired a single proton for each pair of $\mathrm{HSQ}^{-}$ anions.

A similar change of protonation state occurs in (X) (SADRAQ; Braga \& Grepioni, 1998; Fig. 3) which can be classified as a $(-)$ CAHB- $4,4^{\prime}$ chain of $\alpha$-dimers protonated at the $\mathrm{O} 4^{\prime}$ positions according to the equilibrium

$$
\left(\mathrm{HSQ}^{-}\right)_{2}+\mathrm{H}^{+} \rightleftharpoons \mathrm{H}_{2} \mathrm{SQ} \cdot \mathrm{HSQ}^{-}
$$

displayed in (Xb,c).

## 3. Conclusions: crystal chemistry of squaric acid and its anions

The crystal chemistry of squaric acid appears to be rather more complicated than its solution chemistry. In water $\mathrm{H}_{2} \mathrm{SQ}$ behaves as a strong diprotic acid with the formation of both $\mathrm{HSQ}^{-}$and $\mathrm{SQ}^{2-}$ anions. In crystals, however, the $\mathrm{HSQ}^{-}$anion exists in at least four different forms: $\beta$-chain (V), $\alpha$-chain (VI), $\alpha$-dimer (VII) and the $\alpha$-tetramer (VIII). Moreover, in the crystal environment, a third acid anion appears with the same $\mathrm{H}_{2} \mathrm{SQ} \cdot \mathrm{HSQ}^{-}$formula but with two completely different geometries, the first corresponding to the chain of 4 '-protonated $\alpha$-dimers displayed in (Xa), and the second to the $1: 1$ complex of two $\beta$-chains linked in ribbons by very strong $2-2^{\prime}$ -$(-)$ CAHBs shown in (IX).

The various manifestations of squaric acid in crystals cannot, therefore, be explained in terms of the simple chemical classification of its anions, in strict analogy with what happens in the crystal chemistry of silicates, a class of compounds with which squaric acid derivatives seem to have not irrelevant affinities. Squaric acid, $\mathrm{H}_{2} \mathrm{C}_{4} \mathrm{O}_{4}$, has in fact definite topological similarities with the orthosilic acid, $\mathrm{H}_{4} \mathrm{SiO}_{4}$, consisting of a core (the $\mathrm{C}_{4}$ frame or the Si atom) connectable to other nuclei by up to four bonds (four hydrogen bonds or four covalent $\mathrm{Si}-\mathrm{O}-\mathrm{Si}$ bridges). The main differences between the two systems are that:
(i) in space, the squaric acid is a flat (two-dimensional) tecton while the silicic acid is a tetrahedral and then threedimensional one; and
(ii) in projection, the former is tetragonal while the latter is trigonal.
It is reasonable to assume that the crystal chemistry of squarates is a kind of two-dimensional projection of that of silicates with some additional differences due to the tetragonal, instead of trigonal symmetry. This is illustrated in Fig. 11 by representing the $\mathrm{C}_{4} \mathrm{O}_{4}$ frames by simple squares and the hydroxyl positions by dots. In analogy with silicates, the structural motifs include isolated anions (XX) and (XXIV), single- and double-kinked chains (XVIII), (XXI) and (XXIII), ribbons of double chains (XIX) and tetramers (XXII), while the structure of squaric acid (XVII) is the evident topological transformation of the three-dimensional structure of silica into the plane.

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